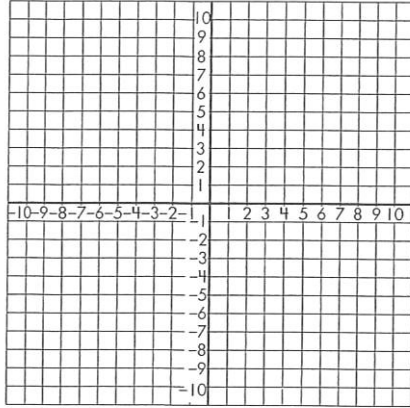


# Lesson 4.9 Graphing Functions

Sketch each linear function shown.

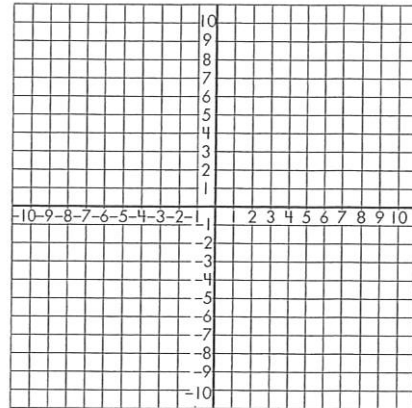
1.

**a**  
 $y = 2x - 1$



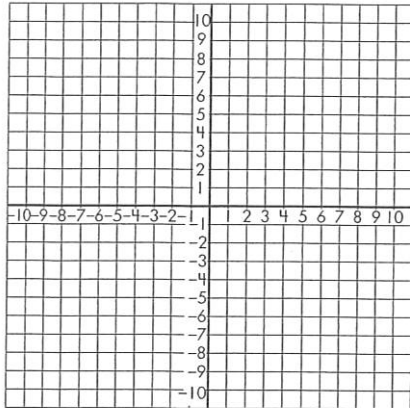
**b**

$$y = -\frac{1}{2}x - 3$$

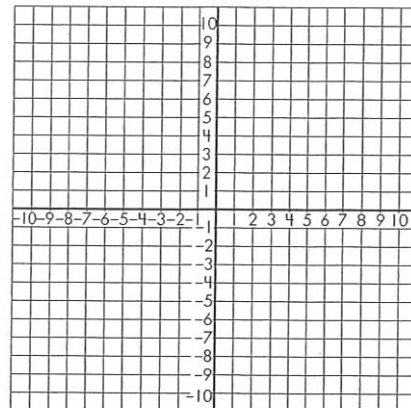


2.

$$y = 3x - 6$$

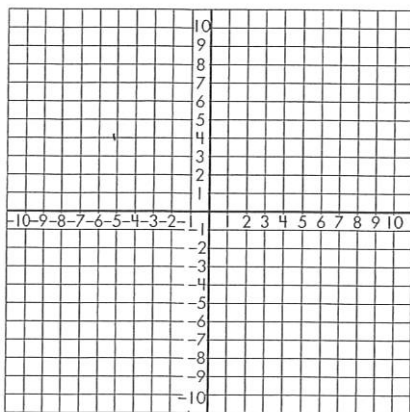


$$y = -\frac{2}{3}x + 4$$

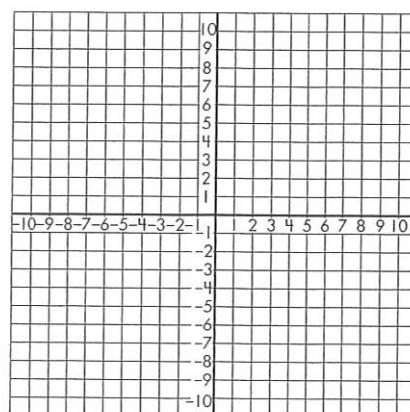


3.

$$y = 4x + 3$$



$$y = -\frac{1}{3}x + 2$$



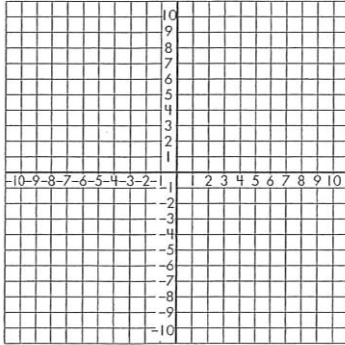
# Lesson 4.9 Graphing Functions

Sketch each linear function shown.

**a**

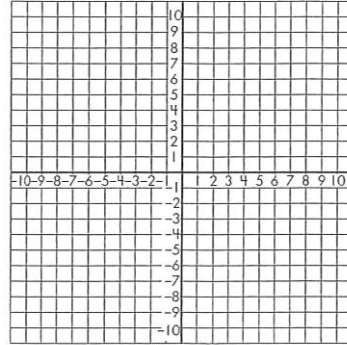
1.

$$y = 3x + 9$$



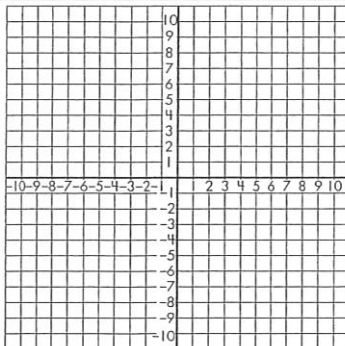
**b**

$$y = 2x - 5$$

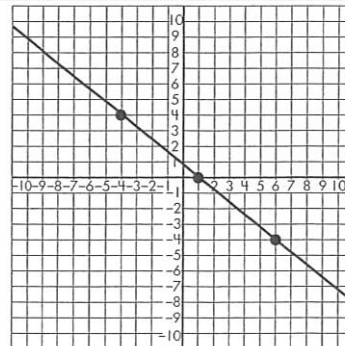


2.

$$y = -3x + 4$$

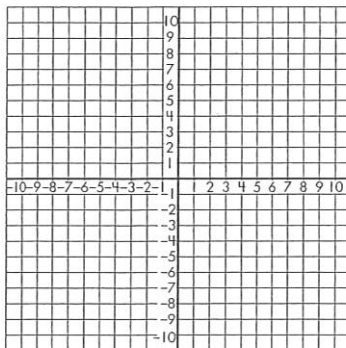


$$y = 5$$

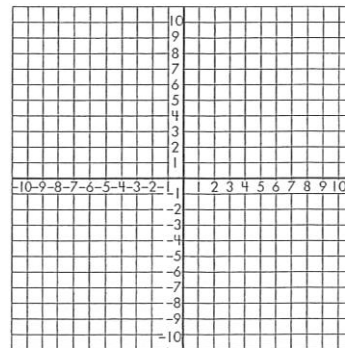


3.

$$y = \frac{1}{2}x + 4$$



$$y = -\frac{4}{5}x + 1$$



Name: \_\_\_\_\_

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**AU4: Notes #1 – Graphing Systems of Equations**

Date: \_\_\_\_\_

**Vocabulary:**

A system of linear equations is \_\_\_\_\_

A solution of a system of linear equations is \_\_\_\_\_

Points of Intersection (POI) are the same thing as the solutions of a system.

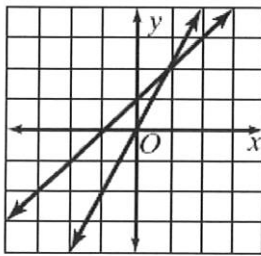
No solution means \_\_\_\_\_

A system of equations has infinitely many solutions when \_\_\_\_\_

**Vocabulary and Key Concepts**

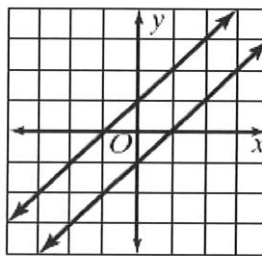
**Numbers of Solutions of Systems of Linear Equations**

different slopes



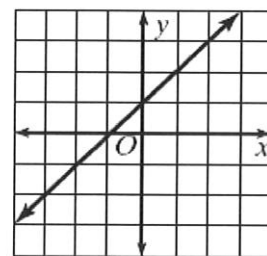
The lines   
so there is  
 solution.

same slope  
different y-intercepts



The lines   
so there are  
 solutions.

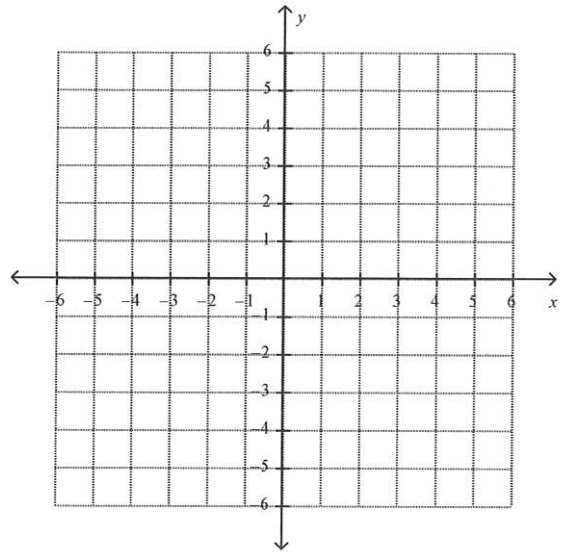
same slope  
same y-intercept



The lines are   
so there are  
  
solutions.

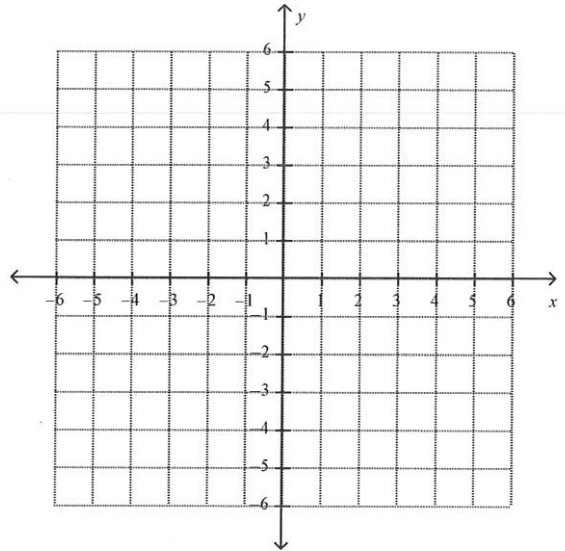
**Solve by graphing:  
Systems with No solutions**

$$1.) \begin{cases} y = 3x + 2 \\ y = 3x - 2 \end{cases}$$

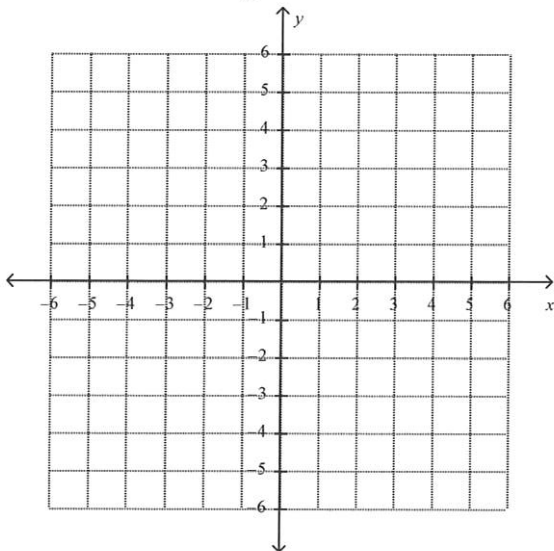


**Systems with Infinitely Many solutions**

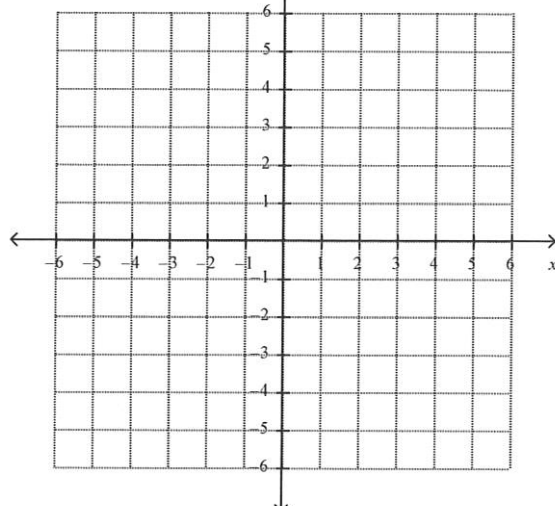
$$2.) \begin{cases} y = -\frac{3}{4}x + 3 \\ y = -\frac{3}{4}x + 3 \end{cases}$$



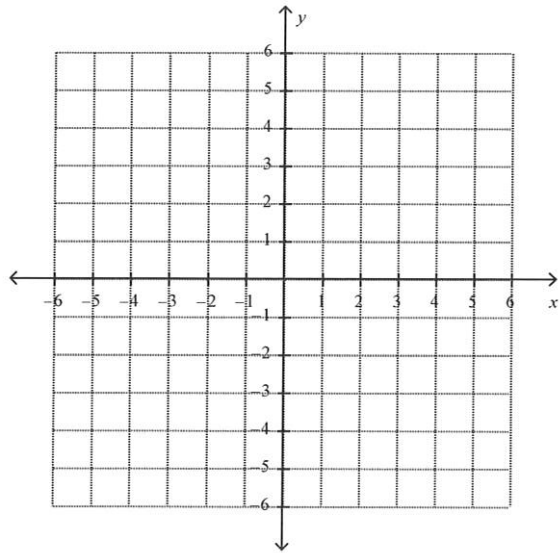
$$\text{Ex. 1) } \begin{cases} y = x + 2 \\ y = 2x + 1 \end{cases}$$



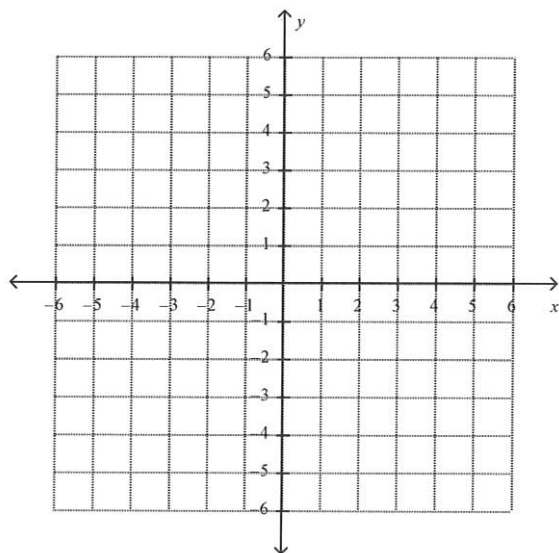
$$\text{Try-It) } \begin{cases} y = -\frac{1}{2}x - 1 \\ y = x - 4 \end{cases}$$



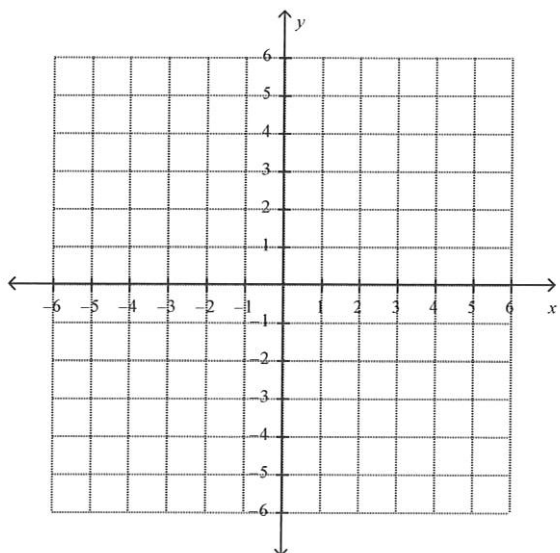
**Ex. 2)**  $\begin{cases} x = 2 \\ y = -6 \end{cases}$



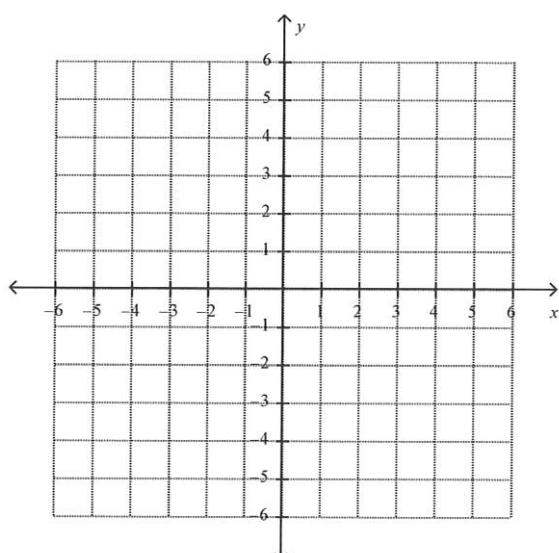
**Try-It)**  $\begin{cases} y = 3 \\ x = -4 \end{cases}$



**Ex. 3)**  $\begin{cases} 2x - 6 = y \\ 3 - x = y \end{cases}$

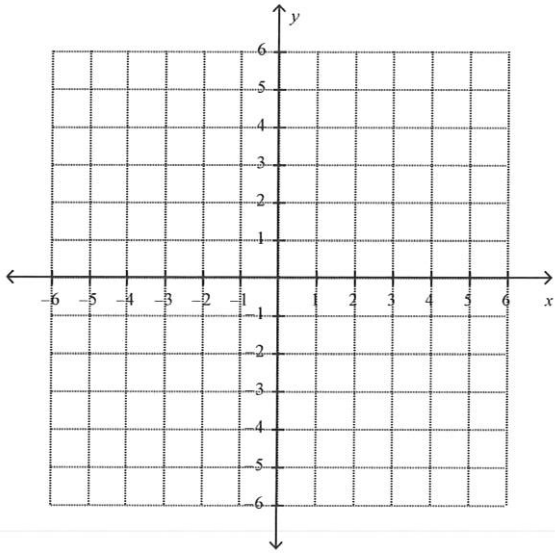


**Try-It)**  $\begin{cases} -\frac{3}{2}x + 2 = y \\ -2 + \frac{1}{2}x = y \end{cases}$

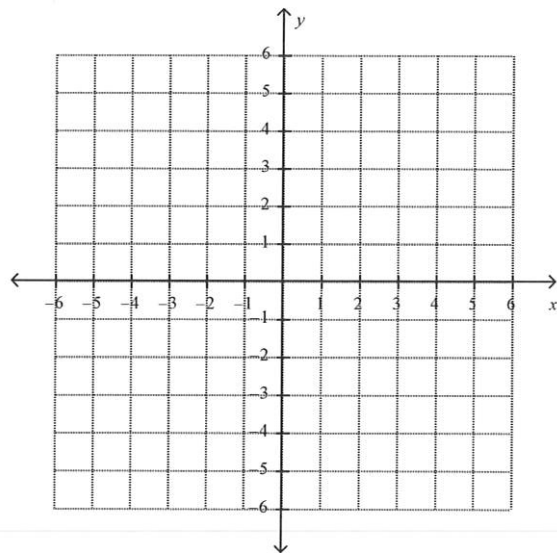


**Graphing Standard Form Systems:**

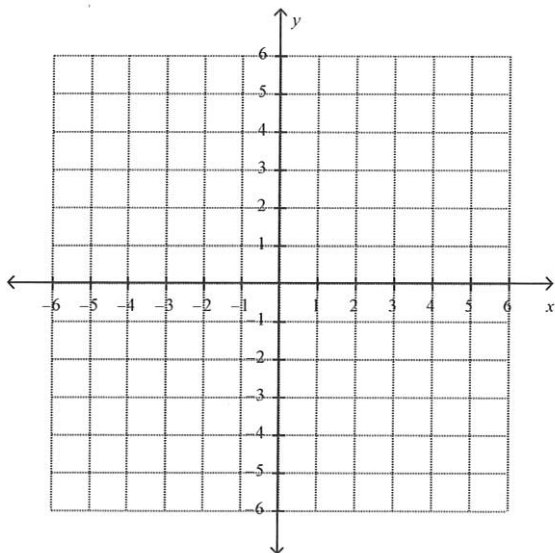
**Ex. 4)** 
$$\begin{cases} x - y = 6 \\ 2x + y = 0 \end{cases}$$



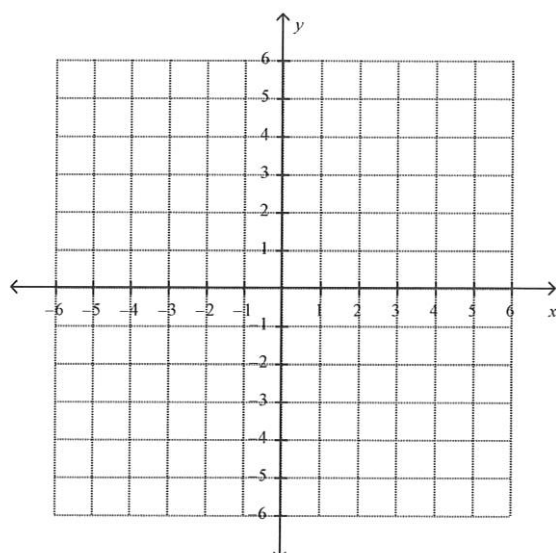
**Try-It)** 
$$\begin{cases} 2x - y = 1 \\ 3x + y = -6 \end{cases}$$



**Try-It)** 
$$\begin{cases} 2x - y = 5 \\ x - y = 1 \end{cases}$$



**Try-It)** 
$$\begin{cases} -2x + y = -5 \\ \frac{1}{3}x + y = 2 \end{cases}$$



Name: \_\_\_\_\_

Class: \_\_\_\_\_

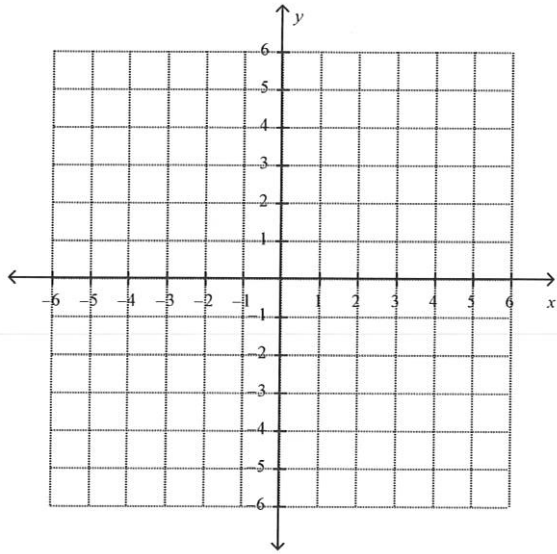
**M8-U5: HW #1 – Graphing Systems of Equations**

Date: \_\_\_\_\_

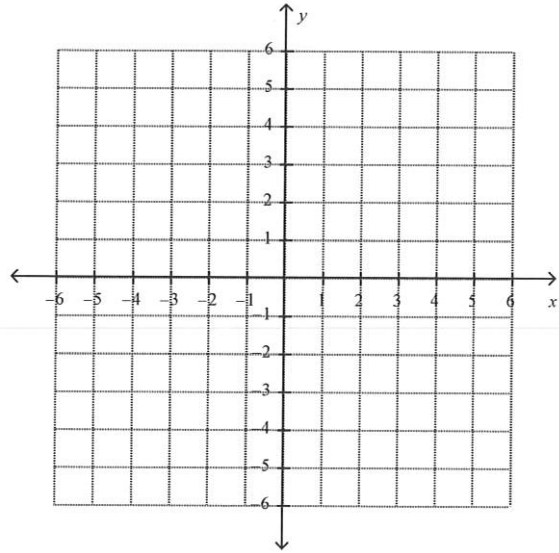
What is the **solution** to the following system of linear equations?

If there is *no solution* or *infinitely many*, explain why.

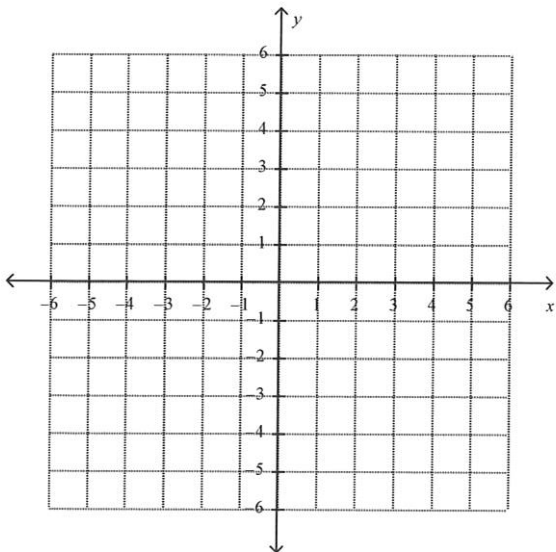
1) 
$$\begin{cases} y = x + 3 \\ y = -2x + 3 \end{cases}$$



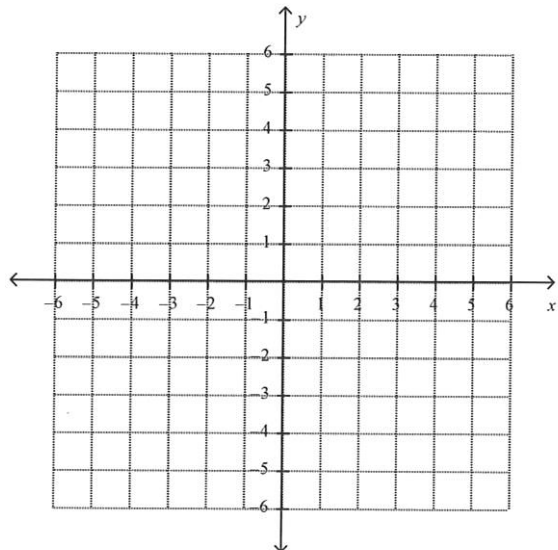
2) 
$$\begin{cases} y = x + 2 \\ y = 4x - 1 \end{cases}$$



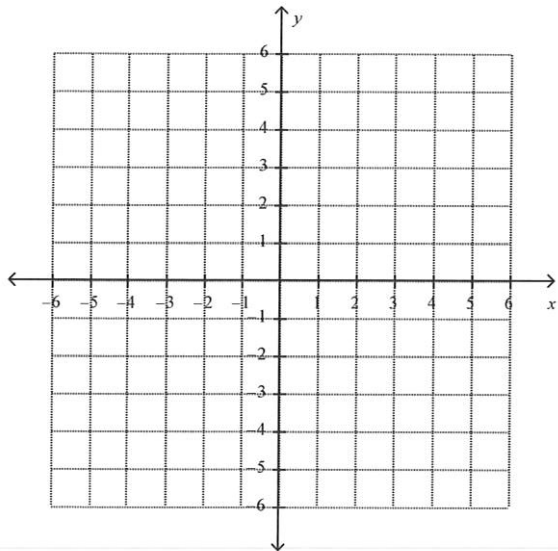
3) 
$$\begin{cases} y = 2x + 3 \\ y = \frac{1}{2}x \end{cases}$$



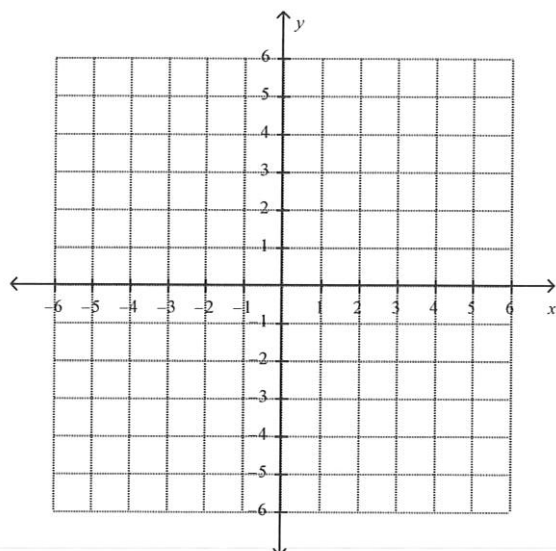
4) 
$$\begin{cases} y = -\frac{3}{2}x + 2 \\ y = \frac{1}{2}x - 2 \end{cases}$$



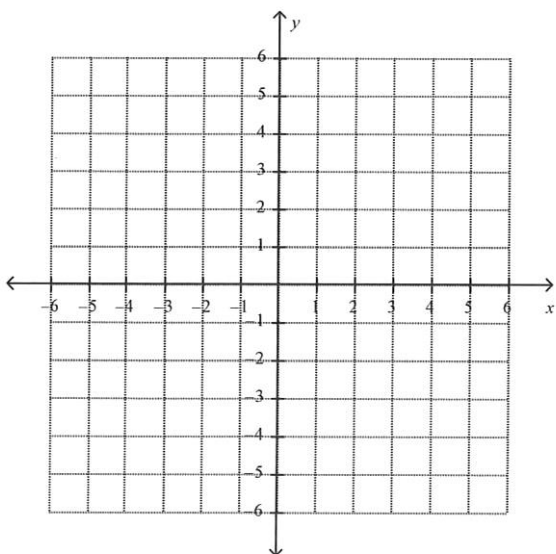
$$5) \begin{cases} x = 5 \\ y = 2 \end{cases}$$



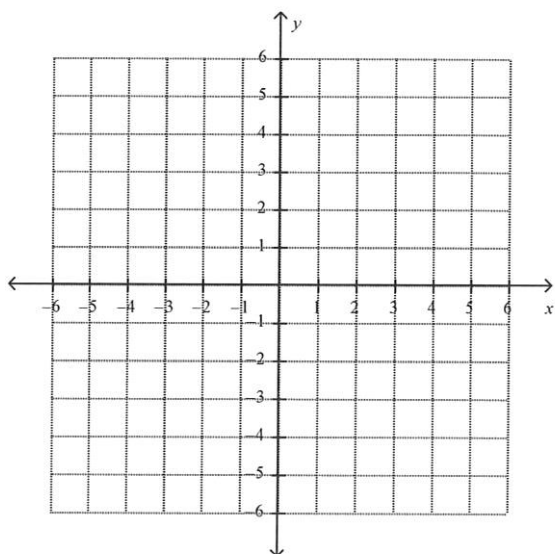
$$6) \begin{cases} 2x - 5 = y \\ -1 + x = y \end{cases}$$



$$7) \begin{cases} y = 2x + 4 \\ y = 2x + 4 \end{cases}$$



$$8) \begin{cases} y = 2x - 2 \\ y = 2x + 5 \end{cases}$$





Name: \_\_\_\_\_

Class: \_\_\_\_\_

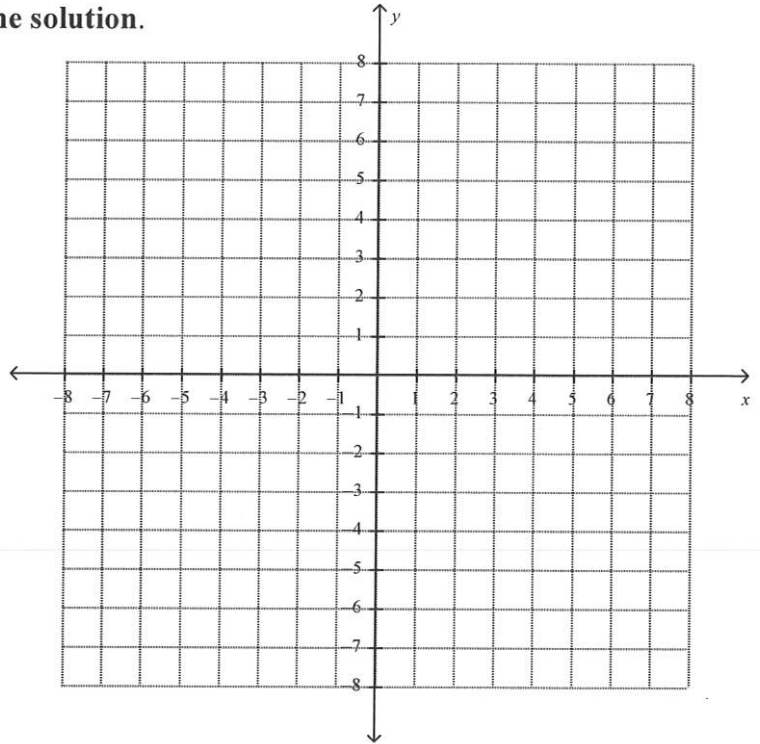
**M8-U5: Notes #2 – Graphing Systems (Day2)**

Date: \_\_\_\_\_

**Warm-Up:**

Graph the two linear equations and **find the solution**.

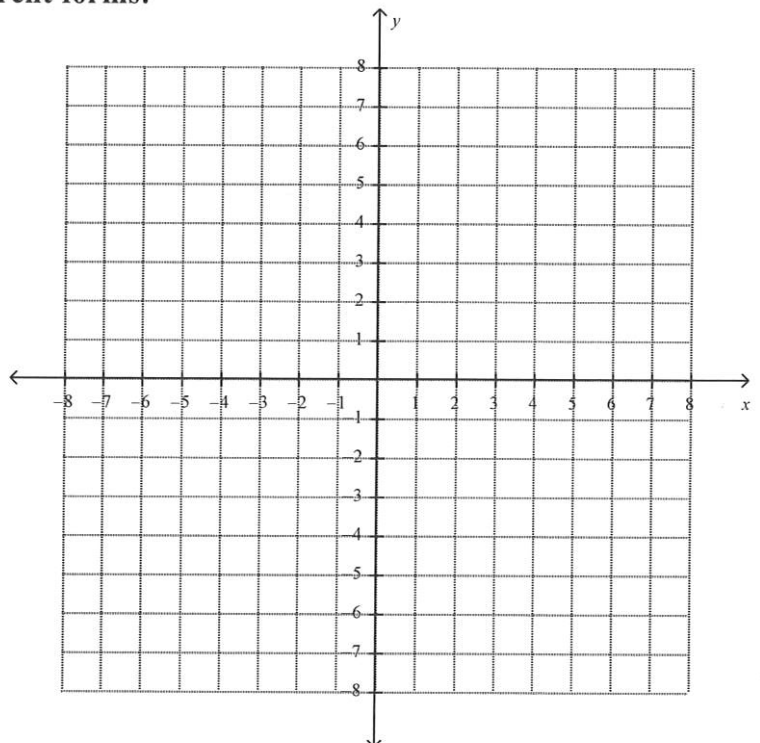
$$\begin{cases} y = -3x + 6 \\ y = -\frac{1}{2}x + 1 \end{cases}$$



**Graphing a system of equations in different forms:**

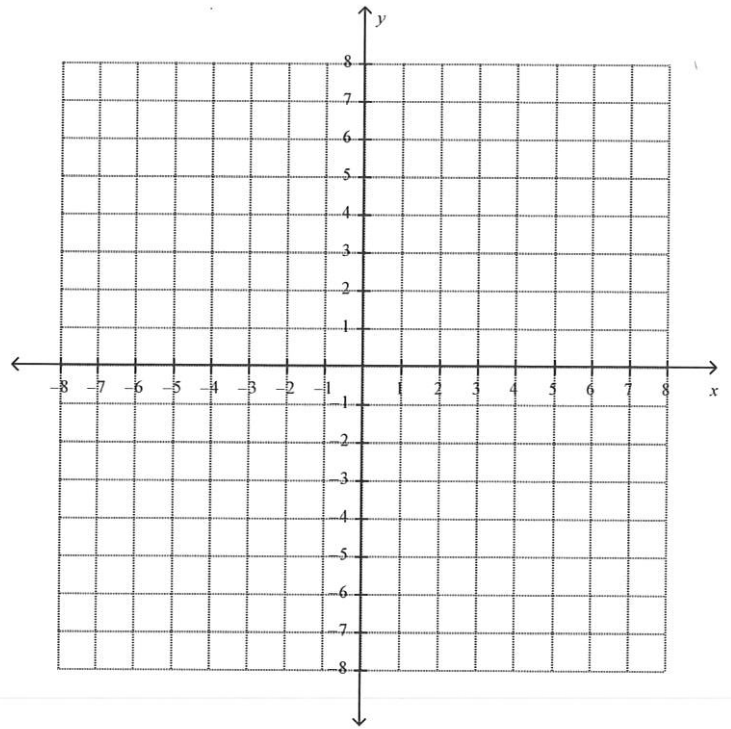
1. Find the solution to the system.

$$\begin{cases} y = 2x - 3 \\ 2x + y = 5 \end{cases}$$



2. Find the solution to the system.

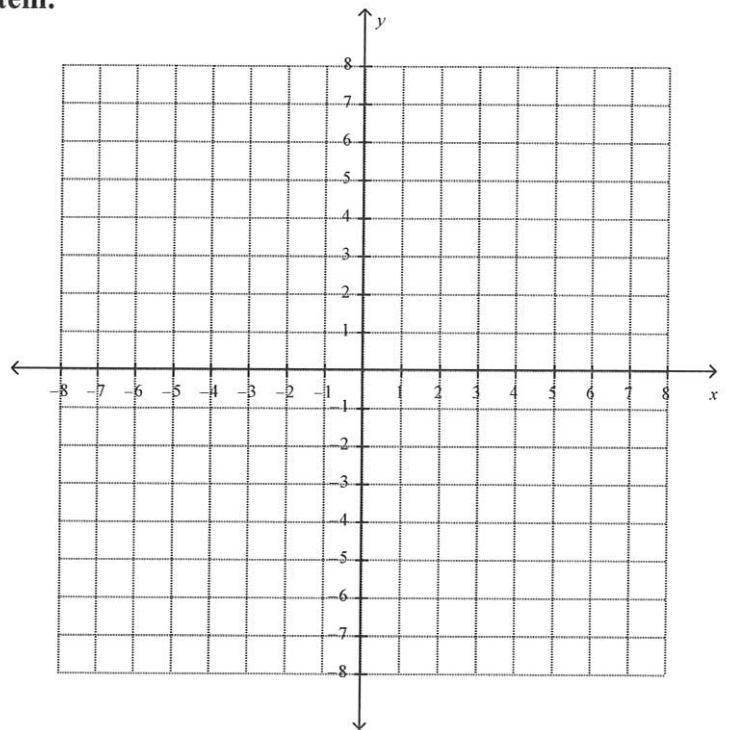
$$\begin{cases} y = -x \\ y + 3 = 2x \end{cases}$$



Try It!

Find the solution the following system.

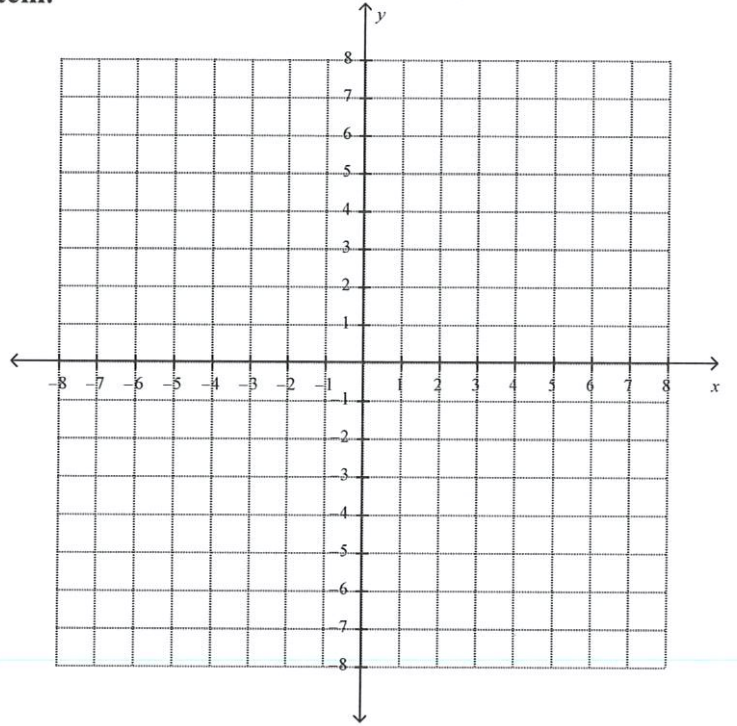
$$\begin{cases} 2x + y = -4 \\ y = 2x + 4 \end{cases}$$



Try It!

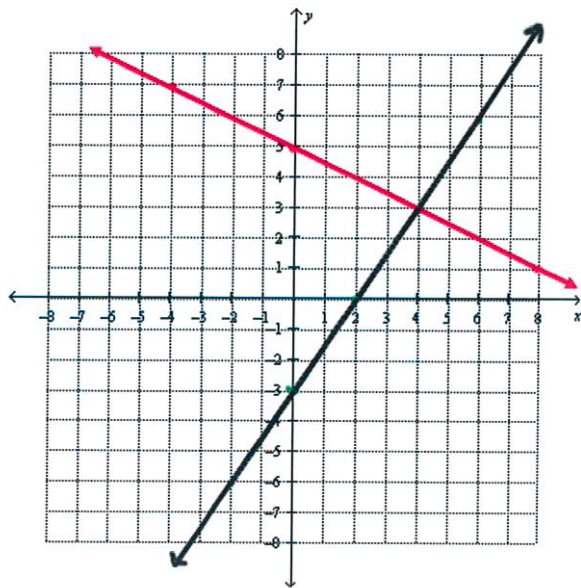
Find the solution the following system.

$$\begin{cases} -4x + y = 1 \\ y = -\frac{1}{2}x + 1 \end{cases}$$

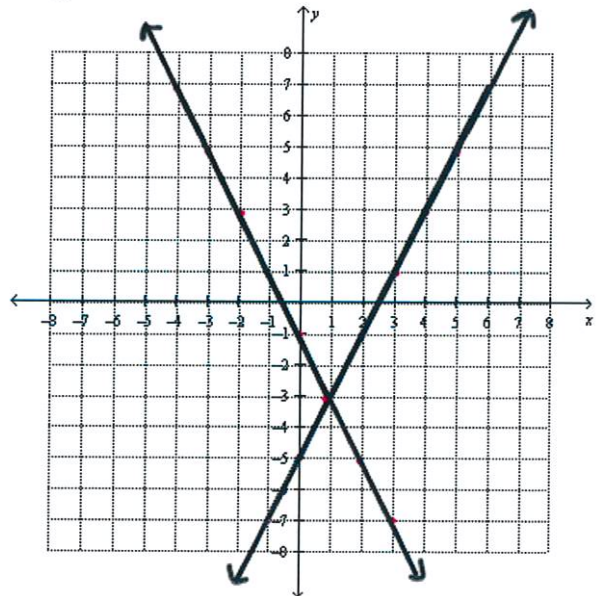


Find the solution to the given systems.

3.

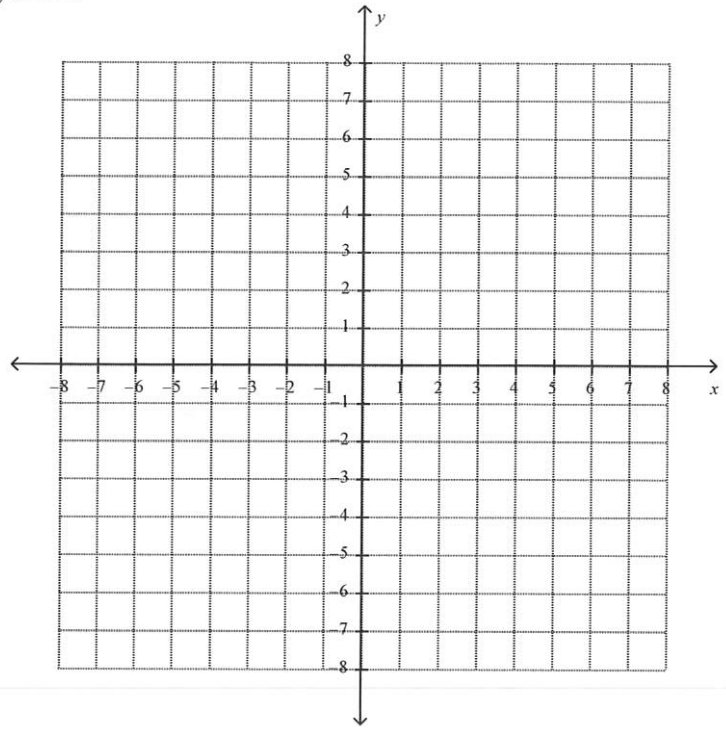


4.



5. Find the solution the following system.

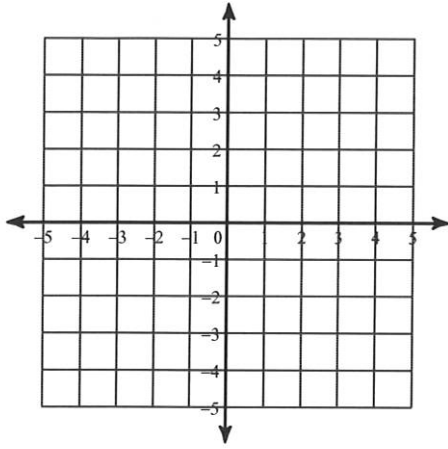
$$\begin{cases} 3x + 4y = 12 \\ y = -\frac{3}{4}x + 3 \end{cases}$$



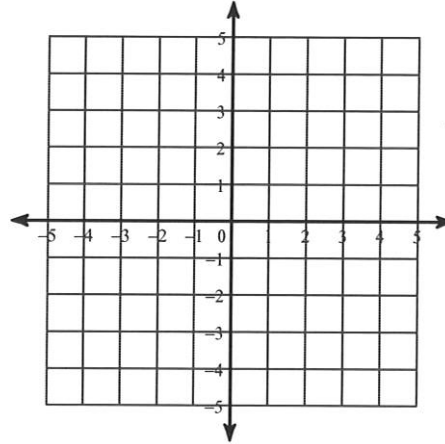
# Solving Systems of Equations by Graphing

Solve each system by graphing (find the point of intersection of the two lines) .

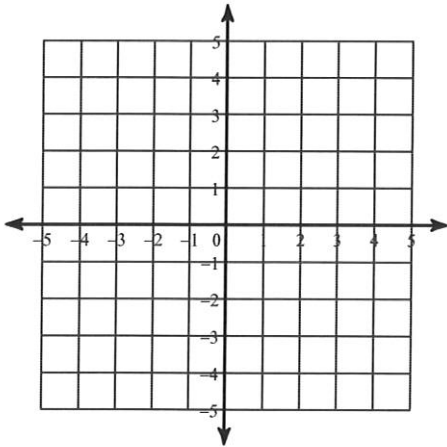
1)  $y = 2x - 3$   
 $y = -3x + 2$



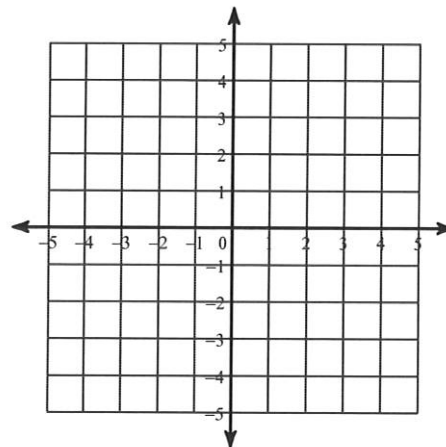
2)  $y = -\frac{5}{3}x + 1$   
 $y = -\frac{1}{3}x - 3$



3)  $y = -x + 1$   
 $x = 3$

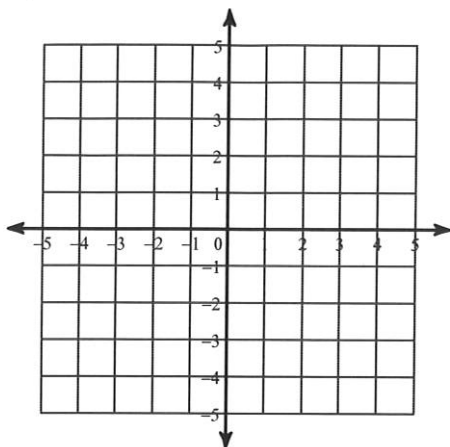


4)  $y = 4x + 1$   
 $y = x - 2$



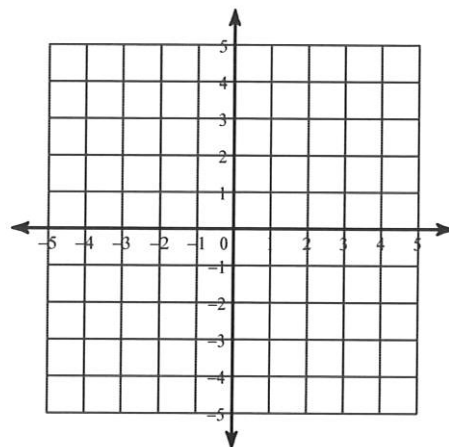
$$5) y = -\frac{1}{3}x + 2$$

$$y = -2x - 3$$



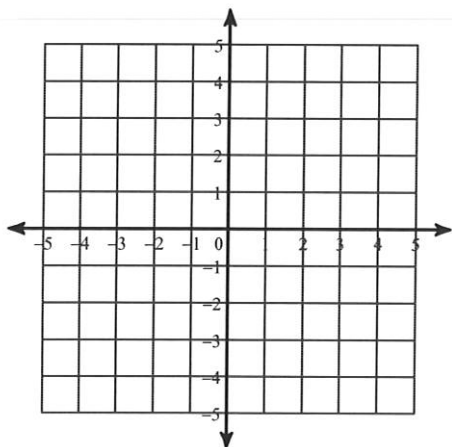
$$6) y = -\frac{1}{4}x + 3$$

$$y = -\frac{3}{2}x - 2$$



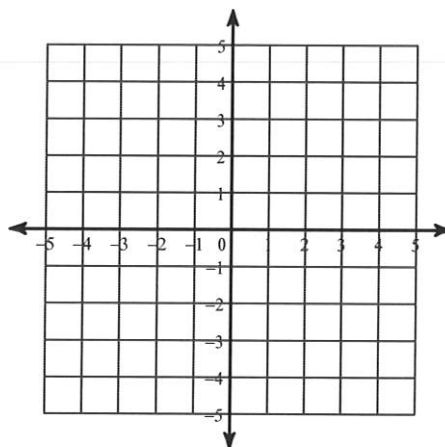
$$7) y = \frac{4}{3}x - 3$$

$$y = 1$$



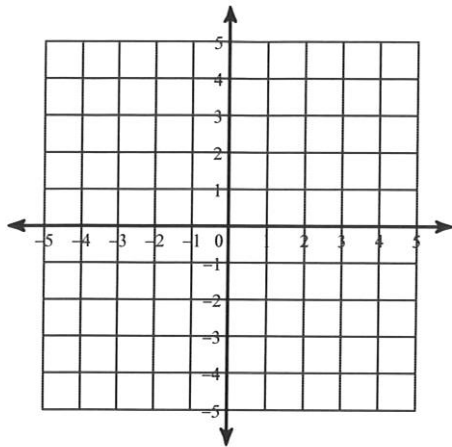
$$8) y = -2x - 4$$

$$y = 4x + 2$$



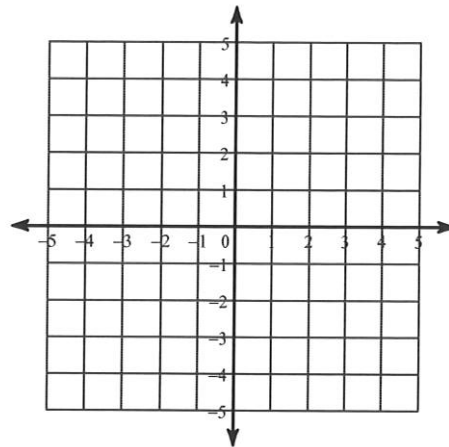
$$9) \ y = -\frac{3}{2}x + 4$$

$$y = \frac{3}{2}x - 2$$



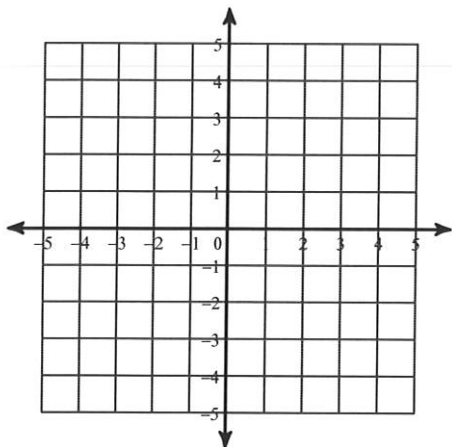
$$10) \ y = 2x - 4$$

$$y = \frac{1}{4}x + 3$$



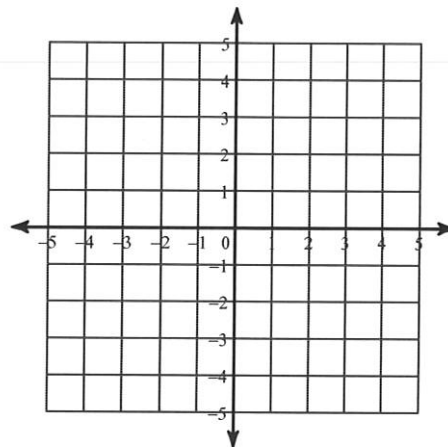
$$11) \ 5x + y = 4$$

$$x - y = 2$$



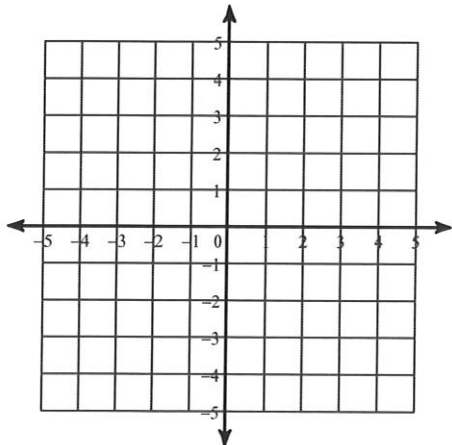
$$12) \ x - 4y = -4$$

$$5x - 4y = 12$$



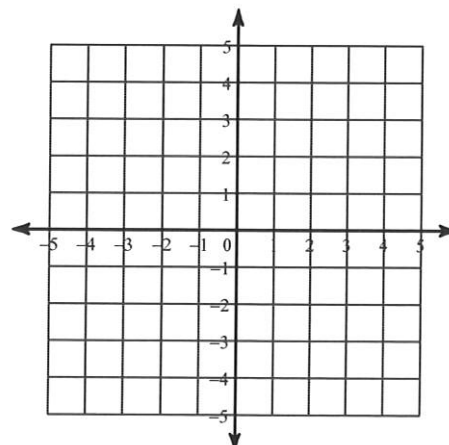
$$13) \ x + y = 3$$

$$8x + y = -4$$

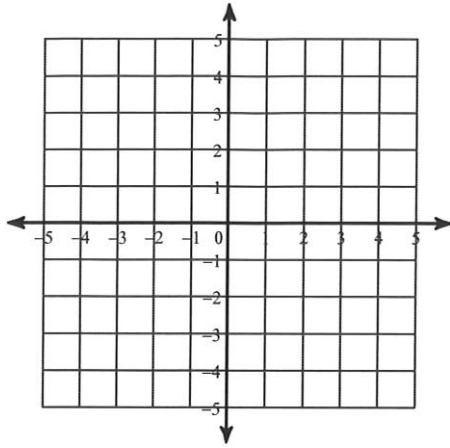


$$14) \ x - y = 2$$

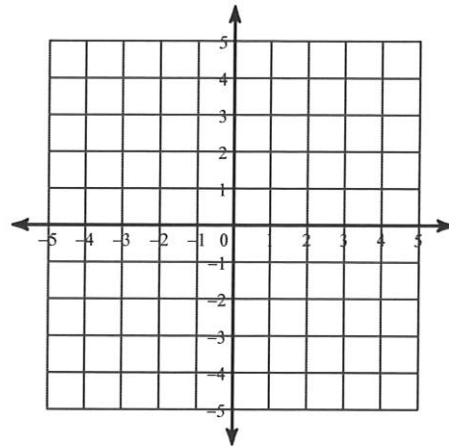
$$x = -2$$



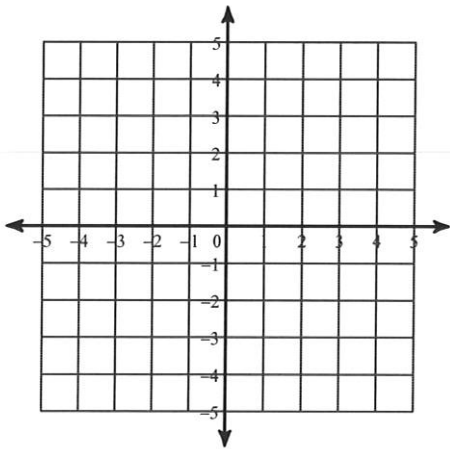
15)  $2x + y = 1$   
 $2x - y = 3$



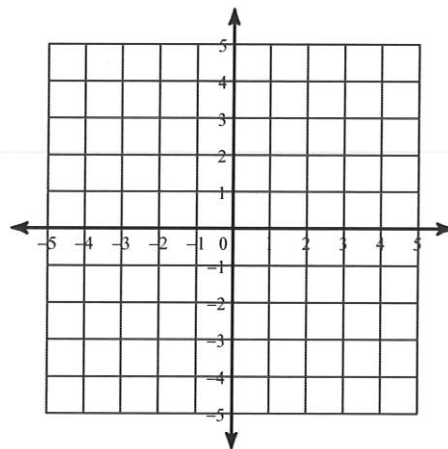
16)  $x - 3y = -6$   
 $2x - y = 3$



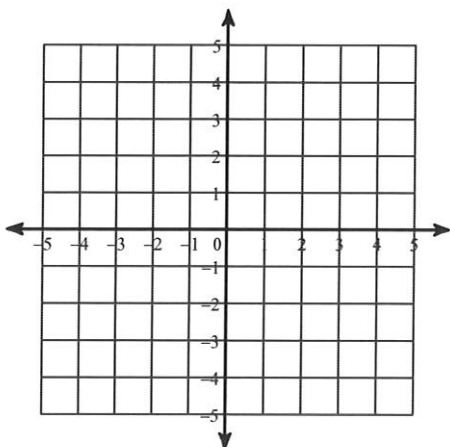
17)  $x + 3y = -12$   
 $5x - 3y = -6$



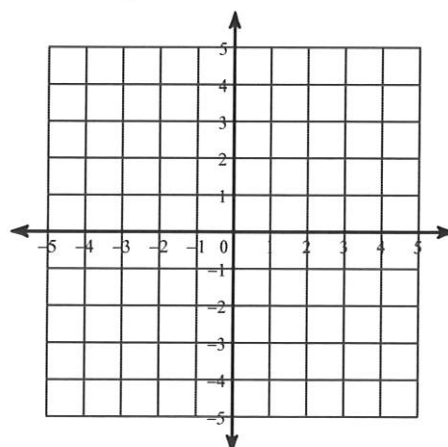
18)  $2x + y = -4$   
 $x + 4y = 12$



19)  $x + 2y = 8$   
 $x - 2y = -4$



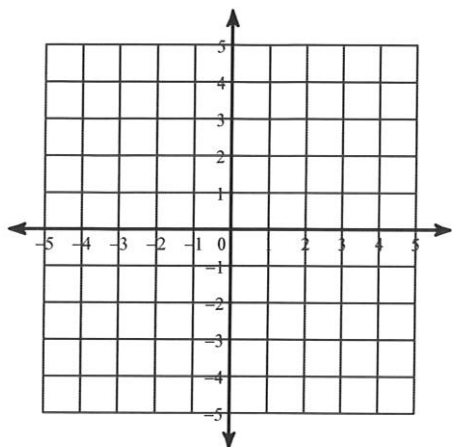
20)  $2x + 3y = -12$   
 $5x - 3y = -9$



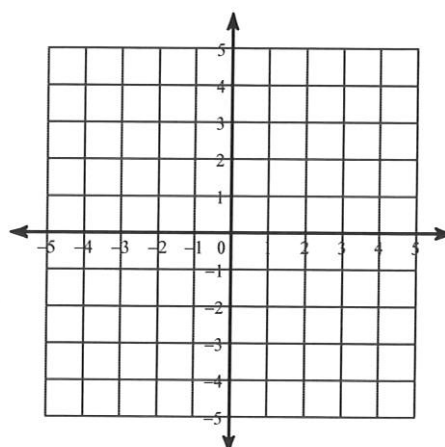


Solve each system by graphing (find the point of intersection of the two lines).

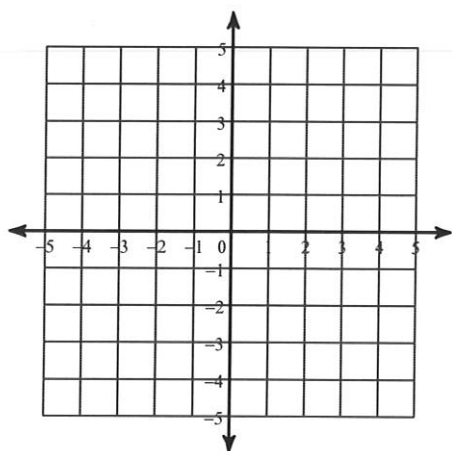
21)  $-6x + y = 4$   
 $-y - 2x = 4$



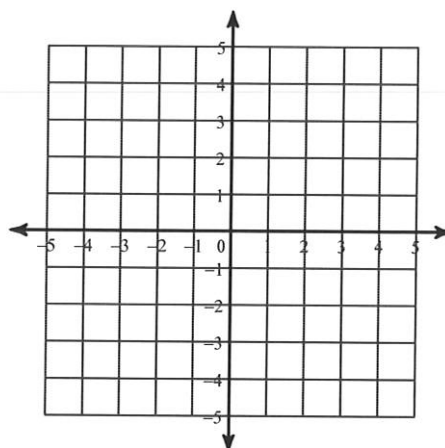
22)  $-y - 3 + 4x = 0$   
 $-4 = -3x - y$



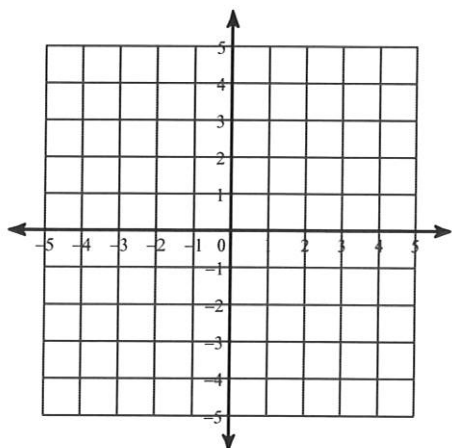
23)  $0 = -3x - 4 - 2y$   
 $2 - \frac{1}{2}x = y$



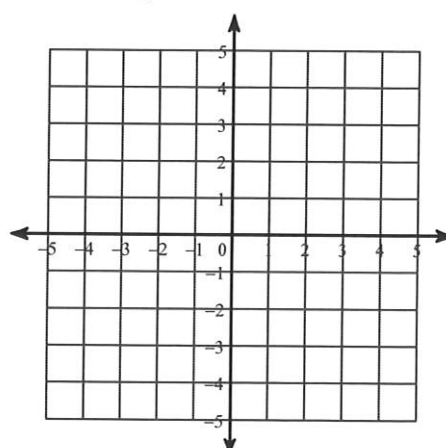
24)  $-2x - y = 1$   
 $-6x = 3y + 3$



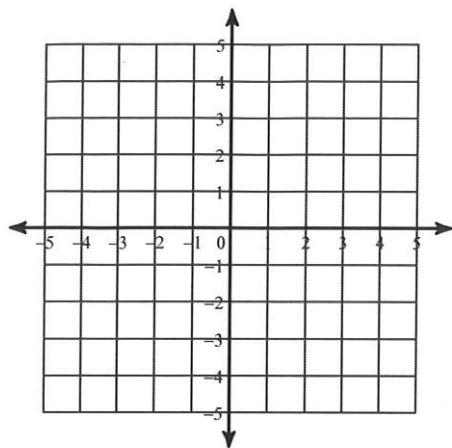
25)  $x - 2y + 8 = 0$   
 $-6 - 2y = -x$



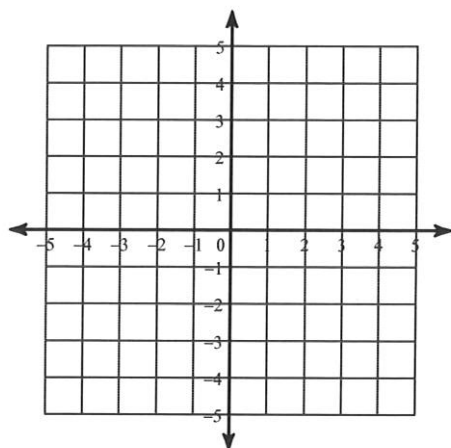
26)  $-2y - 5x = 2$   
 $-5x = 2y - 4$



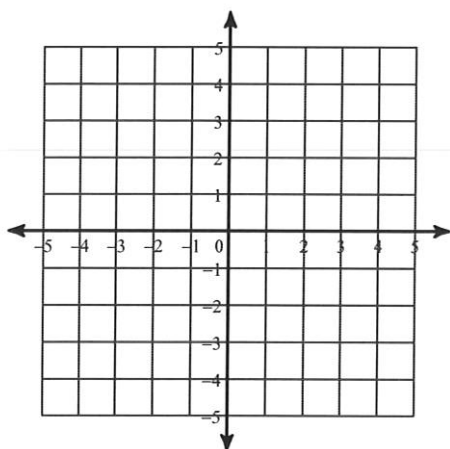
27)  $2y + x - 4 = 0$   
 $2y = -x + 4$



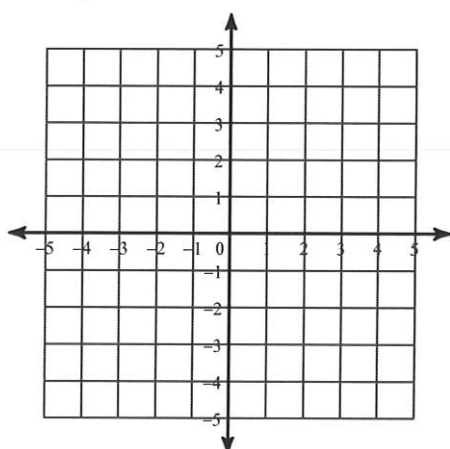
28)  $-4 = -2y$   
 $4 + 6x = -y$



29)  $-2x = -8 - 2y$   
 $-2y - 8 = -2x$



30)  $2y + 4 + 3x = 0$   
 $-2y = 8 + 3x$



Name: \_\_\_\_\_

Class: \_\_\_\_\_

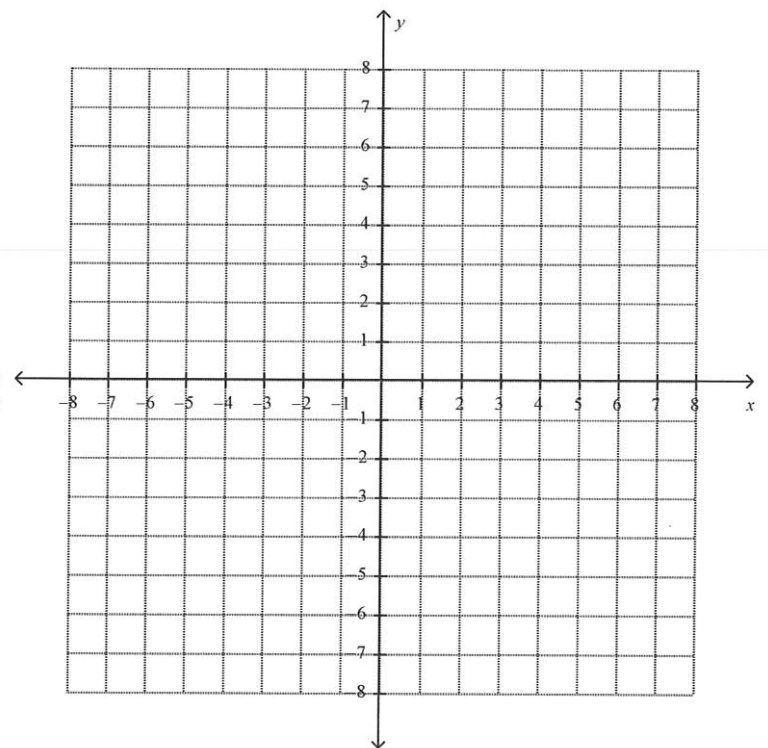
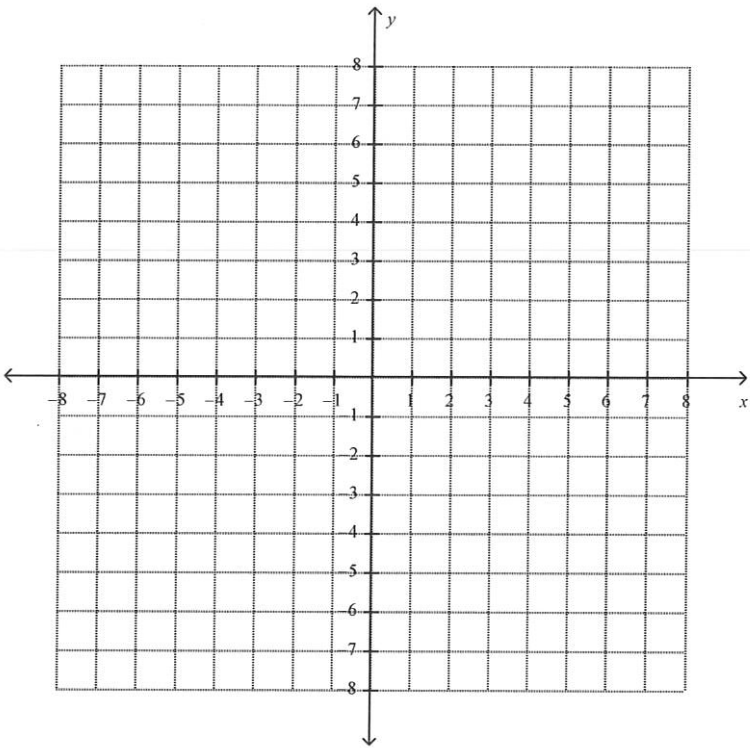
M8-U5: HW #2 – Graphing Systems (Day2)

Date: \_\_\_\_\_

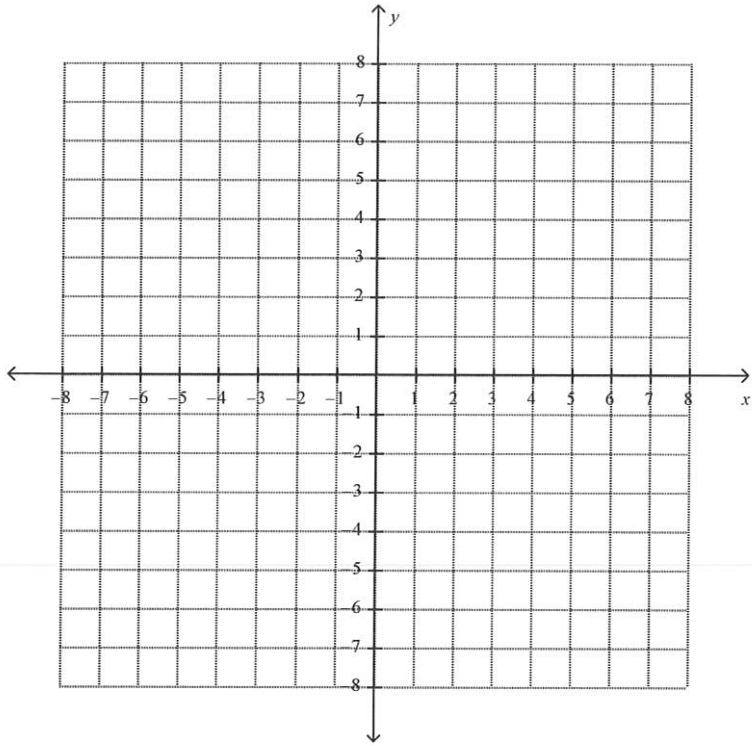
Graph the two linear equations and find the solution.

1. 
$$\begin{cases} y = -x + 2 \\ -x + y = -2 \end{cases}$$

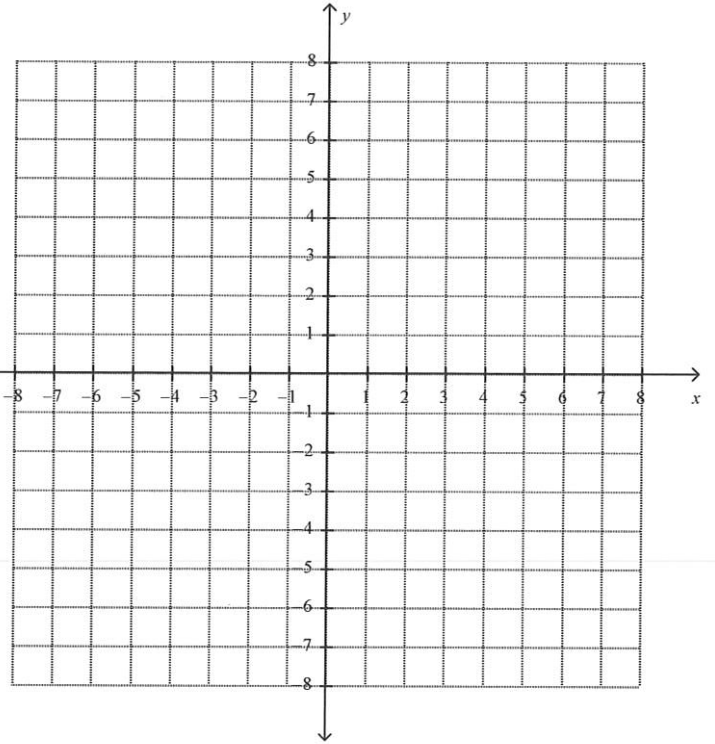
2. 
$$\begin{cases} y = -\frac{1}{4}x - 1 \\ y - 2 = \frac{1}{2}x \end{cases}$$



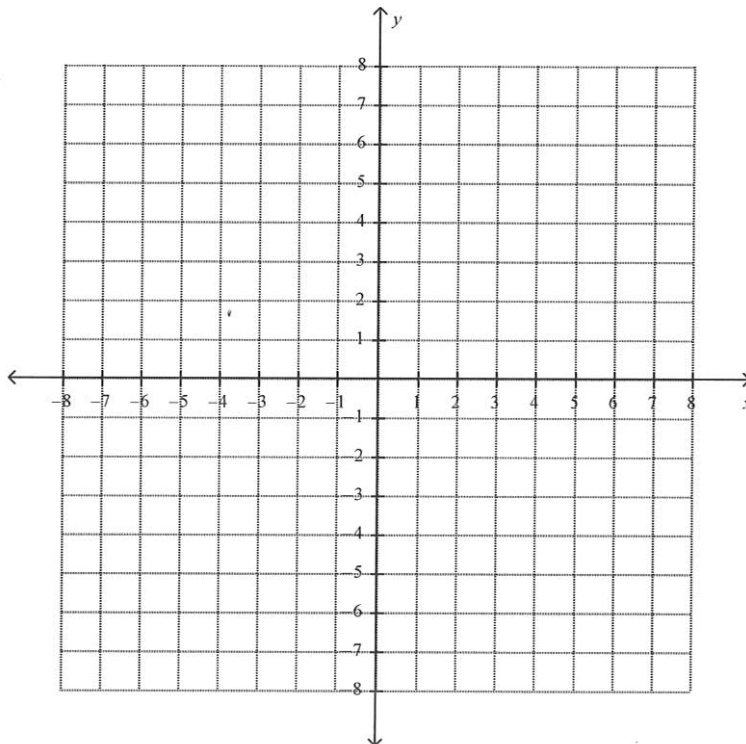
$$3. \begin{cases} y = 2x + 6 \\ -2x + y = 6 \end{cases}$$



$$4. \begin{cases} y - 4 = 2x \\ y - 2x = 4 \end{cases}$$

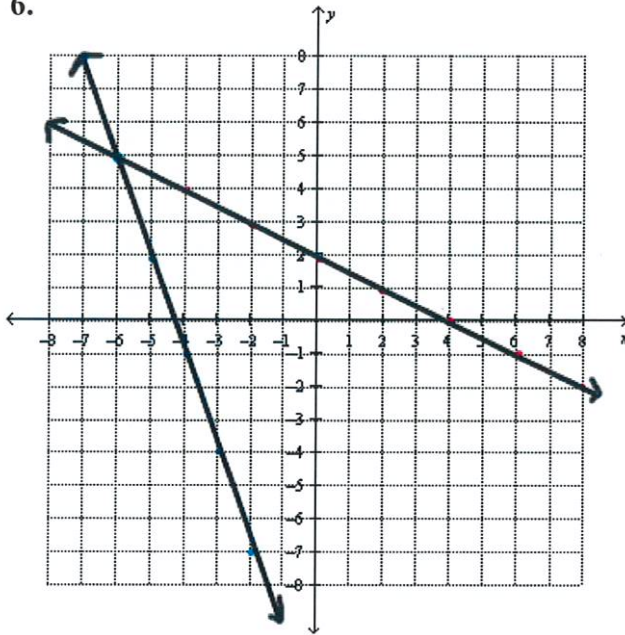


$$5. \begin{cases} 2 + y = 2x \\ y - 2x = 5 \end{cases}$$

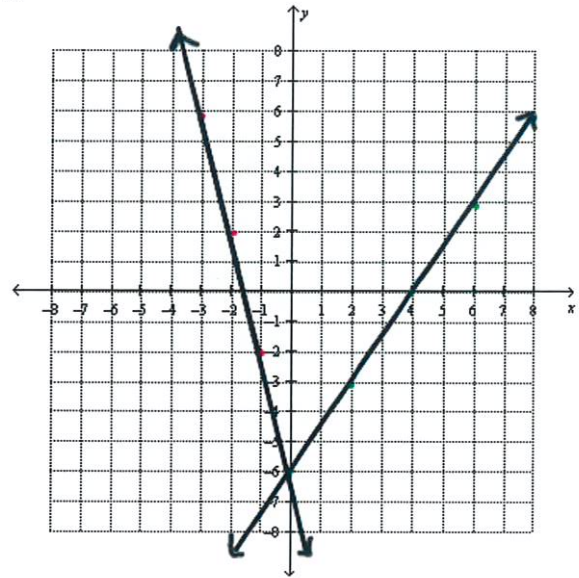


Find the solution to the given systems.

6.



7.



Spiral – Show all work:  
Solve the following equations:

8.  $7k - 8 + 2(k + 12) = 52$

9.  $6(f + 5) = 2(f - 3)$

# Solving Systems Graphically

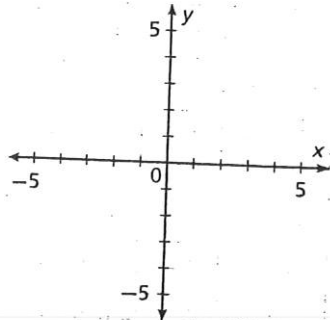
Essential question: *How can you solve a system of equations by graphing?*

COMMON CORE

CC.8.EE.8a  
CC.8.EE.8c

## 1 EXPLORE Investigating Systems of Equations

- A Graph the system of linear functions:  $\begin{cases} y = 3x - 2 \\ y = -2x + 3 \end{cases}$



- B Explain how to tell whether the ordered pair  $(2, -1)$  is a solution of the equation  $y = 3x - 2$  without using the graph.

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- C Explain how to tell whether the ordered pair  $(2, -1)$  is a solution of the equation  $y = -2x + 3$  without using the graph.

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- D Explain how to use the graph to tell whether the ordered pair  $(2, -1)$  is a solution of either equation.

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- E Find an ordered pair that is a solution of both equations. Test the coordinates in each equation to verify your hypothesis.

The point \_\_\_\_\_ is a solution of both equations.

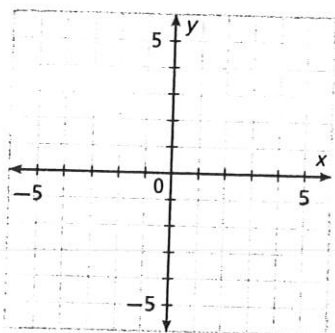
An ordered pair  $(x, y)$  is a solution of an equation in two variables if substituting the  $x$ - and  $y$ -values into the equation results in a true statement. A **system of equations** is a set of equations that have the same variables. An ordered pair is a solution of a system of equations if it is a solution of every equation in the system.

Since the graph of a function represents all ordered pairs that are solutions of the related equation, if a point lies on the graphs of two functions, the point is a solution of both related equations.

## 2 EXAMPLE Solving Systems Graphically

Solve each system by graphing.

A 
$$\begin{cases} y = -x + 4 \\ y = 3x \end{cases}$$



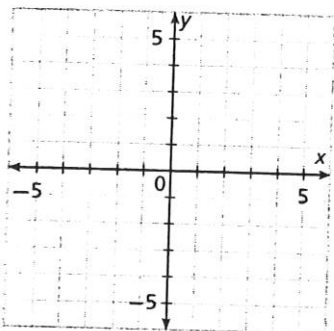
Start by graphing each function.

Identify if there are any ordered pairs that are solutions of both equations.

The solution of the system appears to be \_\_\_\_\_.

To check your answer, you can substitute the values for  $x$  and  $y$  into each equation and make sure the equations are true statements.

B 
$$\begin{cases} y = 2x - 2 \\ y = 2x + 4 \end{cases}$$



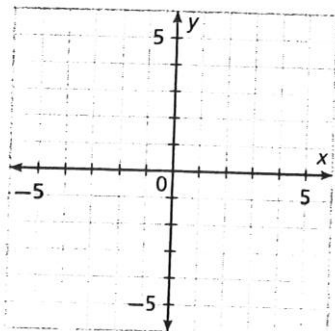
Start by graphing each function.

Identify if there are any ordered pairs that are solutions of both equations.

The graphs are parallel, so there is no ordered pair that is a solution of both equations.

The system has \_\_\_\_\_.

C 
$$\begin{cases} y = 3x - 3 \\ y = 3(x - 1) \end{cases}$$



Start by graphing each function.

Identify if there are any ordered pairs that are solutions of both equations.

The graphs overlap, so every ordered pair that is a solution of one equation is also a solution of the other equation. The system has \_\_\_\_\_.

### 3 EXAMPLE Solving a Real-World Problem by Graphing

Keisha and her friends visit the concession stand at a football game. The stand charges \$2 for a hot dog and \$1 for a drink. The friends buy a total of 8 items for \$11. Tell how many hot dogs and how many drinks they bought.

- A Let  $x$  represent the number of hot dogs they bought and  $y$  represent the number of drinks they bought.

Write an equation representing the **number of items they purchased**.

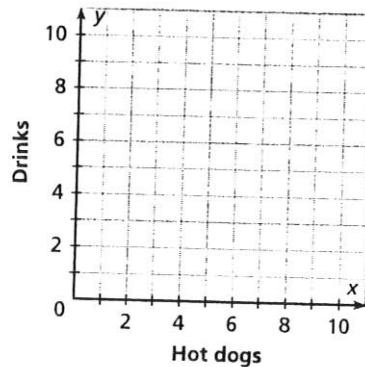
$$\begin{array}{rccccccc} \text{Number of hot dogs} & + & \text{Number of drinks} & = & \text{Total items} \\ & & & & \\ & + & & = & \end{array}$$

Write an equation representing the **money spent on the items**.

$$\begin{array}{rccccccc} \text{Cost of 1 hot dog times} & + & \text{Cost of 1 drink times} & = & \text{Total cost} \\ \text{number of hot dogs} & & \text{number of drinks} & & \\ & + & & = & \end{array}$$

- B Write your equations in slope-intercept form.
- 

- C Graph the solutions of both equations.



- D Use the graph to identify the solution of the system of equations. Check your answer by substituting the ordered pair into both equations.

The point \_\_\_\_\_ is a solution of both equations.

- E Interpret the solution in the original context.

Keisha and her friends bought \_\_\_\_\_ hot dog(s) and \_\_\_\_\_ drink(s).

#### REFLECT

3. **Conjecture** Why do you think the graph is limited to the first quadrant?

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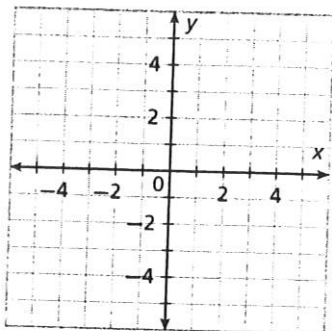
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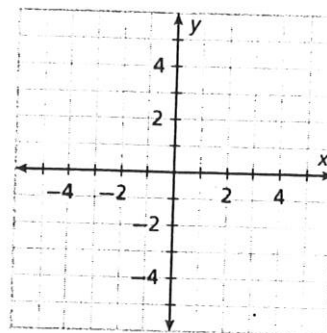
# PRACTICE

Solve each system by graphing.

1. 
$$\begin{cases} 2x - 4y = 10 \\ x + y = 2 \end{cases}$$

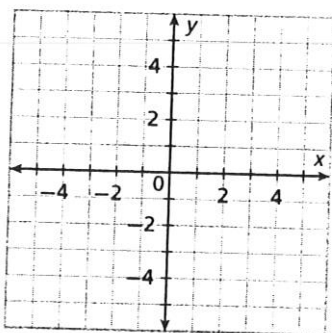


2. 
$$\begin{cases} 2x - y = 0 \\ x + y = -6 \end{cases}$$

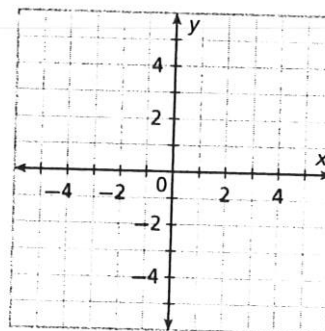


Graph each system and tell how many solutions the system has.

3. 
$$\begin{cases} x - 3y = 2 \\ -3x + 9y = -6 \end{cases}$$



4. 
$$\begin{cases} 2x - y = 5 \\ 2x - y = -1 \end{cases}$$



\_\_\_\_\_ solutions

\_\_\_\_\_ solutions

Mrs. Morales wrote a test with 15 questions covering spelling and vocabulary. Spelling questions ( $x$ ) are worth 5 points and vocabulary questions ( $y$ ) are worth 10 points. The maximum number of points possible on the test is 100.

5. Write an equation in slope-intercept form to represent the number of questions on the test.

\_\_\_\_\_

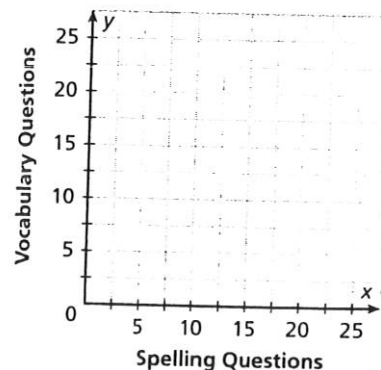
6. Write an equation in slope-intercept form to represent the total points on the test.

\_\_\_\_\_

7. Graph the solutions of both equations.

8. Use your graph to tell how many of each question type are on the test.

\_\_\_\_\_ spelling questions; \_\_\_\_\_ vocabulary questions



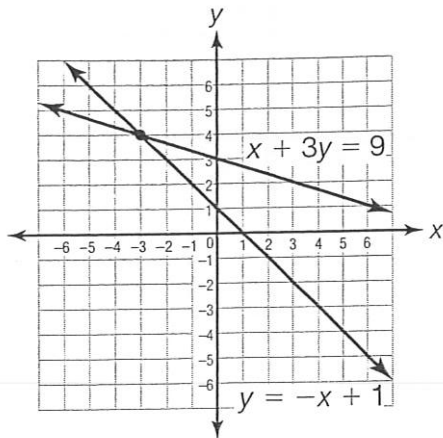
35



## Lesson Practice

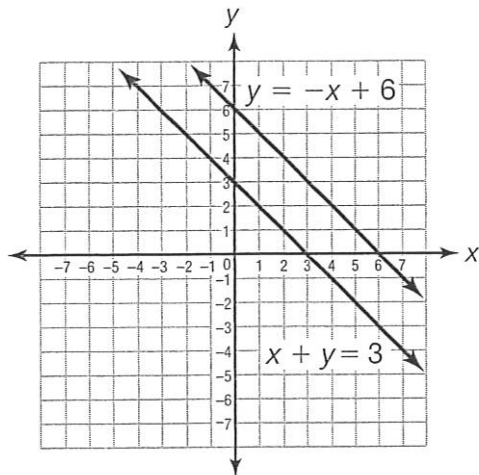
Choose the correct answer.

1. Which is the solution for the system of linear equations graphed below?



- A.  $(-4, 3)$                       C.  $(0, 3)$   
B.  $(0, 1)$                         D.  $(-3, 4)$

2. Which best describes the solution for the system of linear equations graphed below?

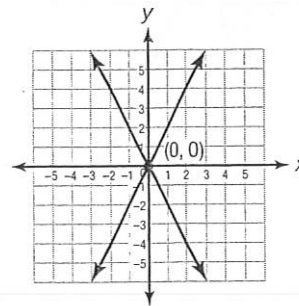


- A.  $(3, 0)$  only  
B.  $(6, 0)$  only  
C. no solution  
D. infinitely many solutions

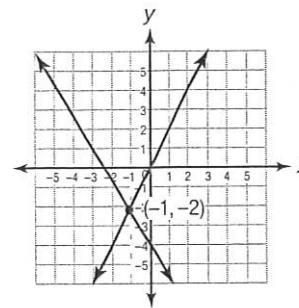
3. Which shows the solution for the following system of equations?

$$y = 2x$$
$$2x + y = -4$$

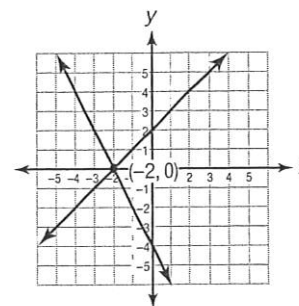
A.



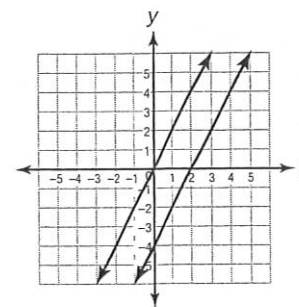
B.



C.



D.



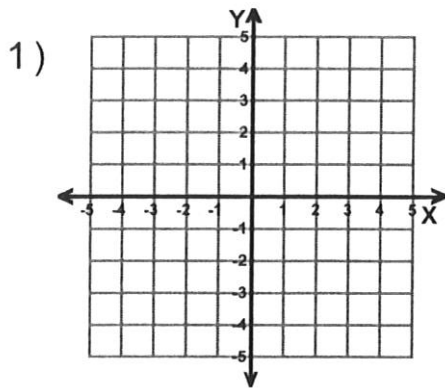
Name : \_\_\_\_\_

Score : \_\_\_\_\_

Teacher : \_\_\_\_\_

Date : \_\_\_\_\_

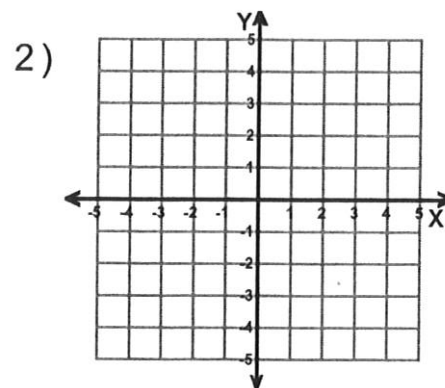
### Solve each system by graphing. Quiz



$$y = -2x + 2$$

$$y = \frac{1}{3}x - 5$$

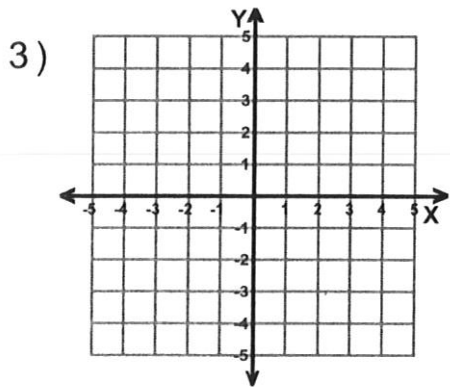
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$$-x + 3y = -6$$

$$-5x + 3y = 6$$

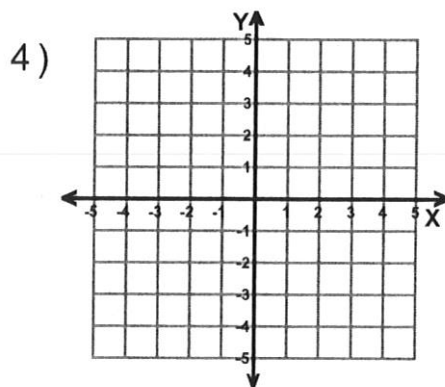
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$$-x + 3y = 6$$

$$4x + 3y = -9$$

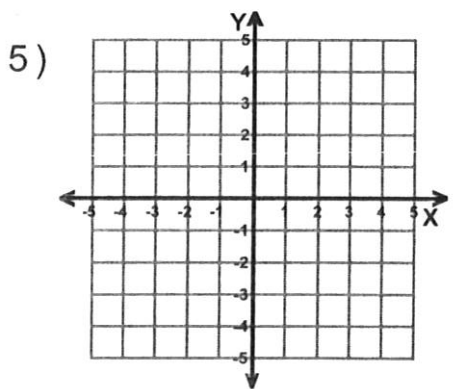
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$$5x + 3y = 12$$

$$-x + 3y = -6$$

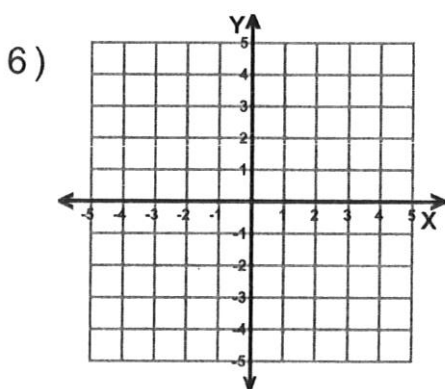
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$$y = \frac{5}{2}x - 4$$

$$y = -x + 3$$

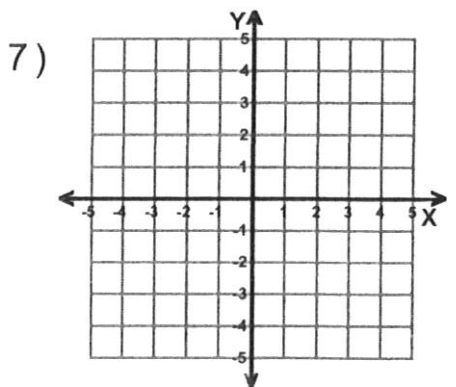
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$$-5x + 2y = 6$$

$$-x + 2y = -2$$

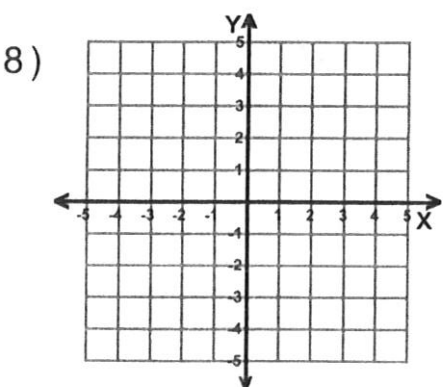
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$$y = \frac{1}{3}x + 2$$

$$y = -\frac{1}{2}x + 2$$

\_\_\_\_\_



$$y = -\frac{4}{9}x - 3$$

$$y = -\frac{7}{5}x - 3$$

\_\_\_\_\_



Name: \_\_\_\_\_

Class: \_\_\_\_\_

**M8-U5: Notes #4 - Solving by Substitution**

Date: \_\_\_\_\_

**Warm-Up:**

Solve this system of equations algebraically.

a. 
$$\begin{cases} y = -2x - 7 \\ y = 2x + 17 \end{cases}$$

b. 
$$\begin{cases} x = -4y + 1 \\ x = y - 4 \end{cases}$$

**Substitution Method:**

The substitution method is another method for solving systems of equations.

1. 
$$\begin{cases} y = x - 2 \\ 2x + 2y = 4 \end{cases}$$

2. 
$$\begin{cases} x = -4y - 4 \\ 3x + 5y = 2 \end{cases}$$

**Try It!**

a. 
$$\begin{cases} y = -2x - 1 \\ x - 2y = 12 \end{cases}$$

b. 
$$\begin{cases} -3x - 7y = 1 \\ y = -2x + 3 \end{cases}$$

**Special Cases**

3. 
$$\begin{cases} y = -3x + 4 \\ 6x + 2y = 7 \end{cases}$$

4. 
$$\begin{cases} y = 3x - 6 \\ -3x + y = -6 \end{cases}$$

**Try It!**

**Solve the following system:**

$$\begin{cases} y = 2x - 5 \\ -2x + y = 7 \end{cases}$$

**Practice: Solve the following systems.**

1. 
$$\begin{cases} 3x - y = 30 \\ y = -x + 14 \end{cases}$$

2. 
$$\begin{cases} x = -6y + 15 \\ -x + 4y = 5 \end{cases}$$

3. 
$$\begin{cases} y = \frac{1}{2}x + 2 \\ x - 2y = -4 \end{cases}$$

Name: \_\_\_\_\_ Core: \_\_\_\_\_

### Solving Systems of Equations through Substitution

Directions: Solve each system using substitution. Write no solution or infinitely many solutions where applicable. Show all your work to receive credit.

1.  $y = x - 9$   
 $2x + 5y = 4$

2.  $4x + 2y = 0$   
 $y = \frac{1}{2}x - 5$

3.  $y = 2x - 4$   
 $7x - 2y = 5$

4.  $-4x + y = 3$   
 $5x - 2y = -9$

5.  $y = 4x - 2$   
 $y = 4x + 1$

6.  $y = x + 3$   
 $y = 5x - 5$

Name: \_\_\_\_\_

Class: \_\_\_\_\_

M8-U5: HW #4 – Solving Systems Using Substitution      Date: \_\_\_\_\_

Solve by substitution. Tell whether the system has *no solution*, *one solution* or *infinitely many solutions*.

1. 
$$\begin{cases} y = x + 4 \\ y = 3x \end{cases}$$

2. 
$$\begin{cases} x = -2y + 1 \\ x = y - 5 \end{cases}$$

3. 
$$\begin{cases} y = 5x + 5 \\ y = 15x - 1 \end{cases}$$

4. 
$$\begin{cases} y = x - 7 \\ 2x + y = 8 \end{cases}$$



$$5. \begin{cases} y = 3x - 6 \\ -3x + y = -6 \end{cases}$$

$$6. \begin{cases} x + 2y = 200 \\ x = y + 50 \end{cases}$$

$$7. \begin{cases} 2x + y = 3 \\ y = 2x + 1 \end{cases}$$

$$8. \begin{cases} y = \frac{3}{2}x \\ 6x - 4y = 1 \end{cases}$$